

Numerical simulation of overhead power line cooling in natural convection regime



Gregor Kosec
Jure Slak

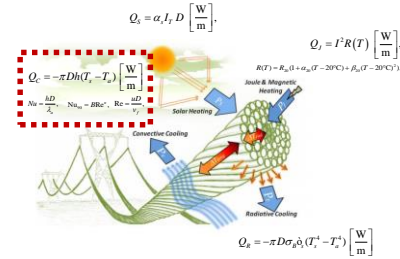
Jožef Stefan Institute (JSI)



Scope

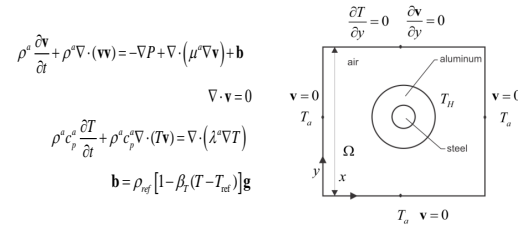
Cooling of conductor due to the natural convection

The most important cooling mechanism of a conductor, i.e. convection, is, in all standard Dynamic Thermal Rating (DTR) models, taken into account in terms of empirical relation that are mostly based on data collected by Morgan in 1975.



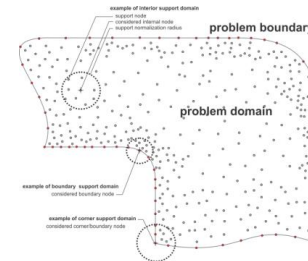
Physical model

The domain of the problem is a cross-section of a power line that is further separated into a steel core and aluminum conductor, and surrounding air



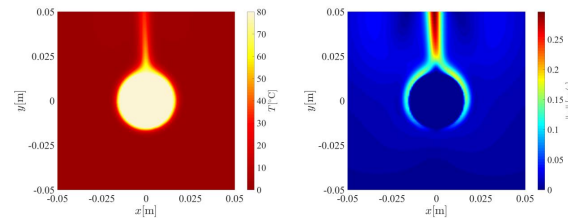
Numerical solution

The solution procedure is divided in two time loops, namely the air and the power line loop. The involved Partial Differential Equations are discretized with RBF-FD method.



Results

The results of the simulation are presented in terms of temperature and velocity magnitude contour plots, convergence analyses, and comparison of convective heat losses of simulated results to IEC, IEEE and CIGRE standards.





Numerical model vs. CIGRE/IEEE

Numerical solution of temperature and velocity fields around conductor

- Steady state achieved in order of 1 s
- Temporal discretization in order of 1 ms

CIGRE and IEEE assume empirical relation between temperature and cooling rate

In numerical model we solve thermo-fluid problem and compute cooling rate without any parameters.

Computation of heat generation and transport within the power line

- Steady state achieved in order of 10 min
- Temporal discretization in order of 10 s

CIGRE in IEEE assume homogenous conductor and assess the skin and core temperature from closed form solution of simplified problem.

In numerical model we compute 2D simulation of heat transfer and generation within the power line.

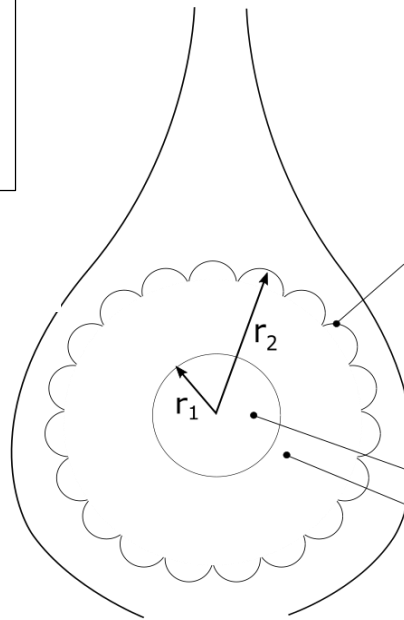
Natural convection:
Thermo-fluid problem

$$\rho^a \frac{\partial \mathbf{v}}{\partial t} + \rho^a \nabla \cdot (\mathbf{v}\mathbf{v}) = -\nabla P + \nabla \cdot (\mu^a \nabla \mathbf{v}) + \mathbf{b}$$

$$\nabla \cdot \mathbf{v} = 0$$

$$\rho^a c_p^a \frac{\partial T^a}{\partial t} + \rho^a c_p^a \nabla \cdot (T^a \mathbf{v}) = \nabla \cdot (\lambda^a \nabla T^a)$$

$$\mathbf{b} = \rho_{ref} [1 - \beta_T (T^a - T_{ref})] \mathbf{g}$$



Radiation
Boundary condition

$$q_R = \sigma_B \epsilon_s (T_{al}^4(r_2) - T_a^4) \left[\frac{\text{W}}{\text{m}^2} \right]$$

$$q_s = \frac{\alpha_s I_T}{\pi} \left[\frac{\text{W}}{\text{m}^2} \right],$$

Steel part – heat transport

$$T^{al}(r_1) = T^{st}(r_1)$$

Aluminium part – heat transport and heat generation

$$\rho^{st} \frac{\partial T^{st}}{\partial t} = \lambda^{st} \nabla^2 T^{st}$$

$$c_p^{al} \rho^{al} \frac{\partial T^{al}}{\partial t} = \lambda^{al} \nabla^2 T^{al} + q_j$$

$$q_j = \frac{I^2 R(T^{al})}{S^{al}} \left[\frac{\text{W}}{\text{m}^3} \right],$$

$$\lambda^{al} \frac{\partial T^{al}}{\partial \mathbf{n}} \Big|_{r_1} = \lambda^{st} \frac{\partial T^{st}}{\partial \mathbf{n}} \Big|_{r_1}$$

$$\lambda^{al} \frac{\partial T^{al}}{\partial \mathbf{n}} \Big|_{r_2} - \lambda^a \frac{\partial T^a}{\partial \mathbf{n}} \Big|_{r_2} = q_s + q_r$$

$$T^{al}(r_2) = T^a(r_2)$$



Solution procedure

Main simulation loop

$$c_p^{st} \rho^{st} \frac{\partial T^{st}}{\partial t} = \lambda^{st} \nabla^2 T^{st}$$

Implicit solution of heat transport in steel part

$$c_p^{al} \rho^{al} \frac{\partial T^{al}}{\partial t} = \lambda^{al} \nabla^2 T^{al} + \frac{I^2 R(T)}{S^{al}}$$

Implicit solution of heat transport and generation in aluminum part

$$\mathbf{v}^i = \mathbf{v}_1 + \Delta t_a \left(\frac{1}{\rho^a} \nabla \cdot (\mu^a \nabla \mathbf{v}) - \nabla \cdot (\mathbf{v} \mathbf{v}) + \frac{\mathbf{b}}{\rho_a} \right)$$

Explicit solution of intermediate velocity

$$\nabla^2 p^c = \frac{\rho}{\Delta t_{air}} \nabla \cdot \mathbf{v}^i$$

$$\frac{\partial p}{\partial n} = (\nabla \cdot (\mu^a \nabla \mathbf{v}) + \mathbf{b}) \cdot \hat{\mathbf{n}}$$

Pressure correction
Poisson equation with regularization

$$\int_{\Omega} p d\Omega = 0$$

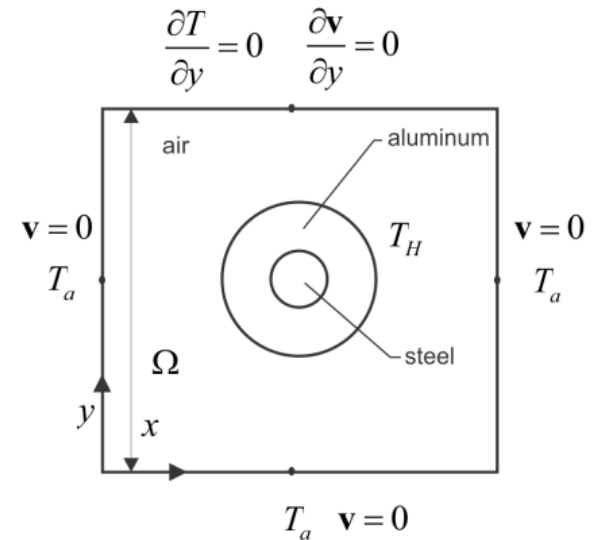
$$\mathbf{v}_2 = \mathbf{v}_1 - \frac{\Delta t_a}{\rho} \nabla p^c$$

Velocity correction

$$T_2 = T_1 + \Delta t_a \left(\frac{1}{\rho^a c_p^a} \nabla \cdot (\lambda^a \nabla T) - \nabla \cdot (T \mathbf{v}_1) \right)$$

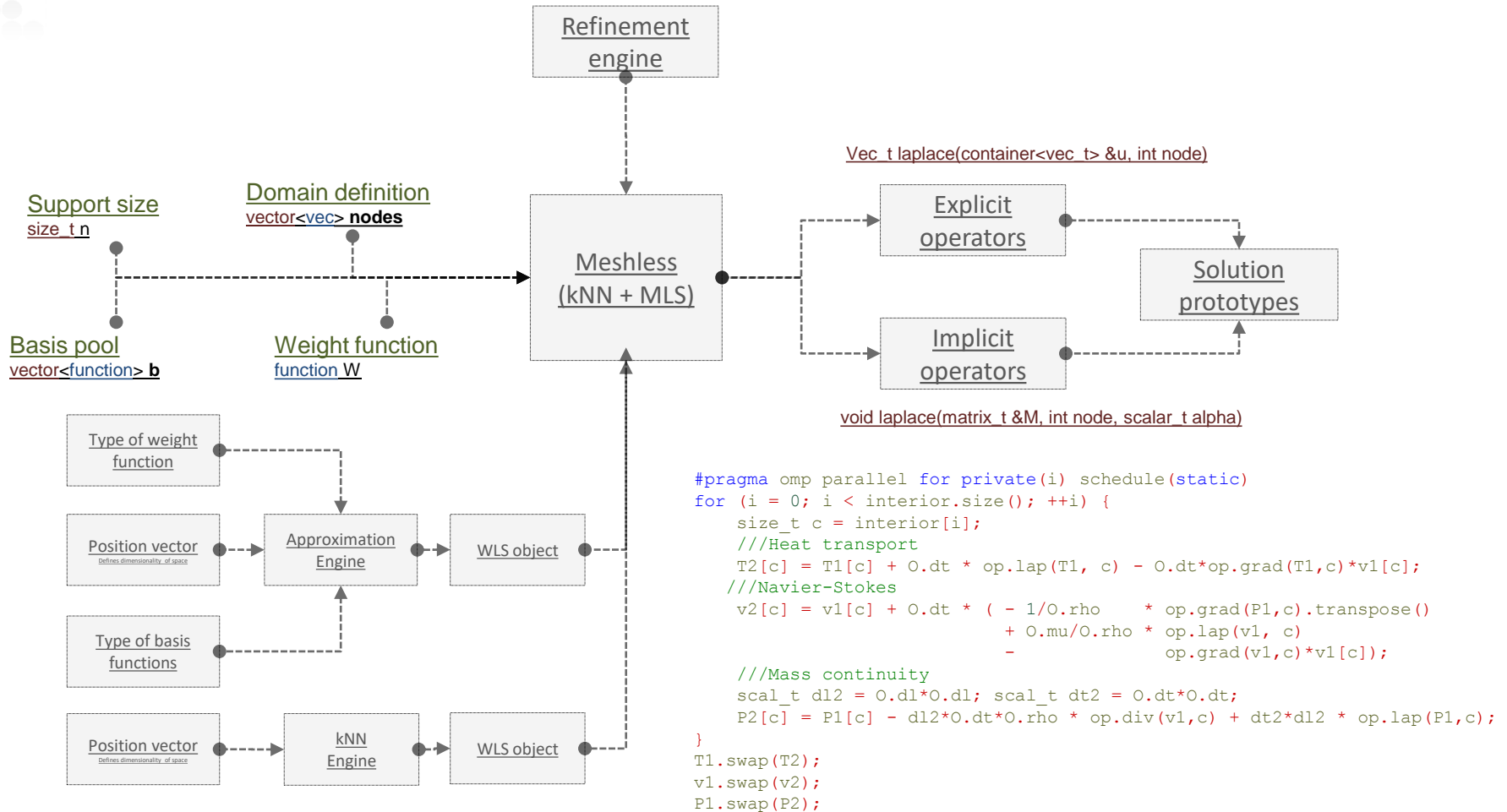
Explicit time advance of heat transport

Internal loop – Thermo fluid problem





Implementation



open source meshless project

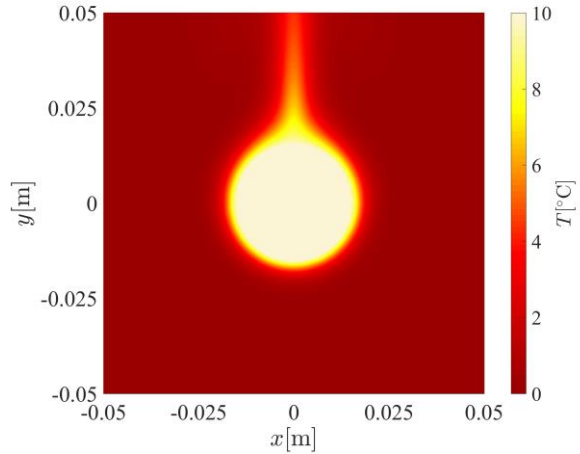
Medusa: Coordinate Free Meshless Method implementation (MM)

<https://gitlab.com/e62Lab/medusa> | <http://e6.ijs.si/medusa/>

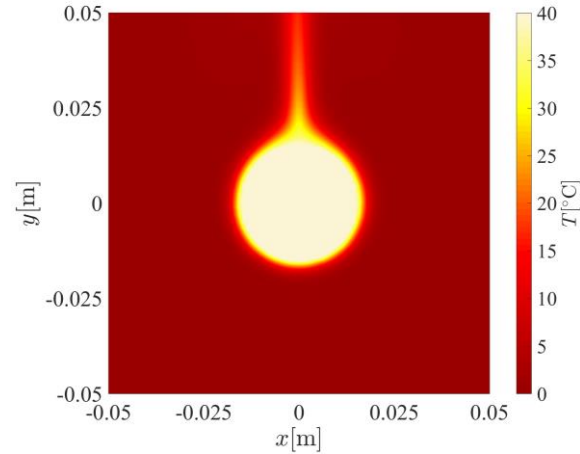


Simulation of natural convection from Al490Fe65 conductor

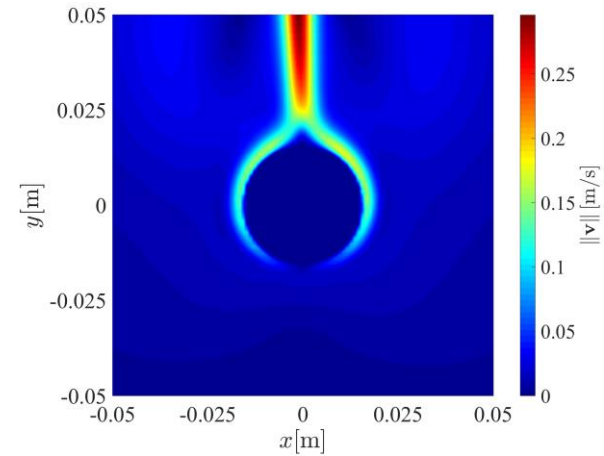
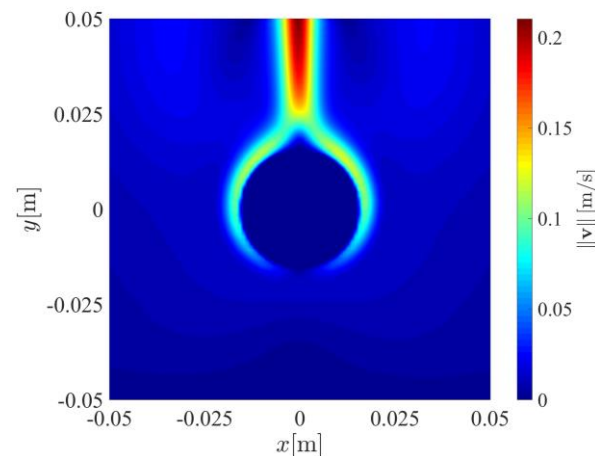
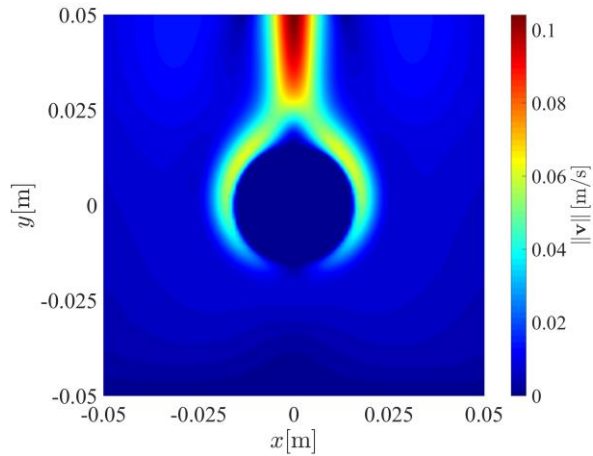
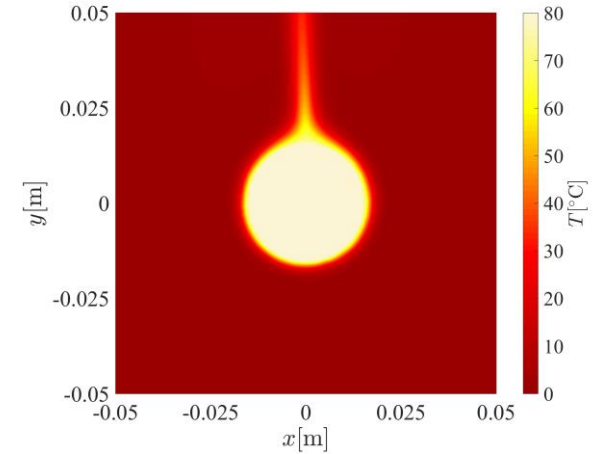
$\Delta T = 10^\circ\text{C}$

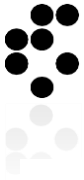


$\Delta T = 40^\circ\text{C}$

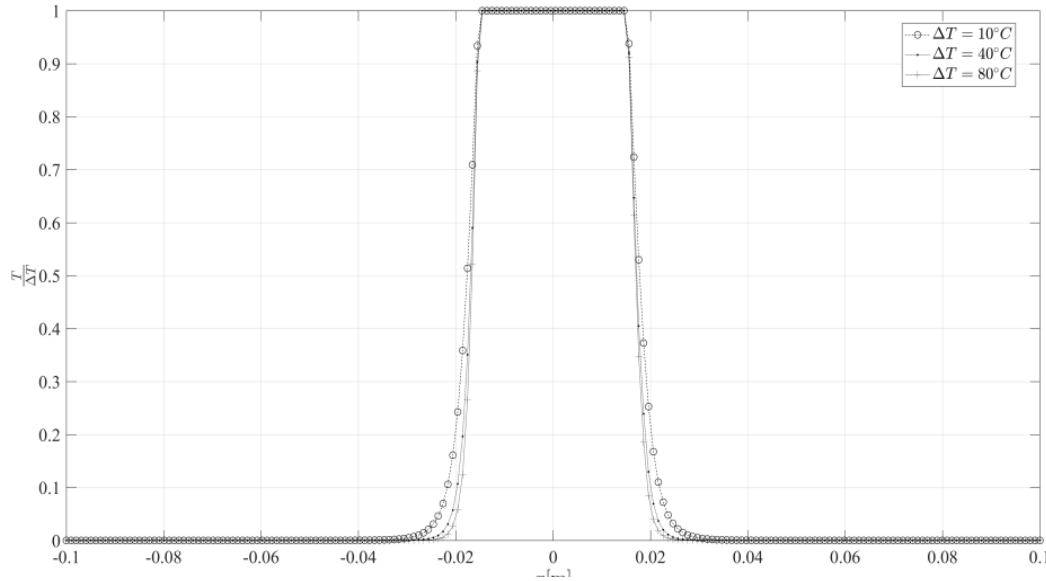


$\Delta T = 80^\circ\text{C}$

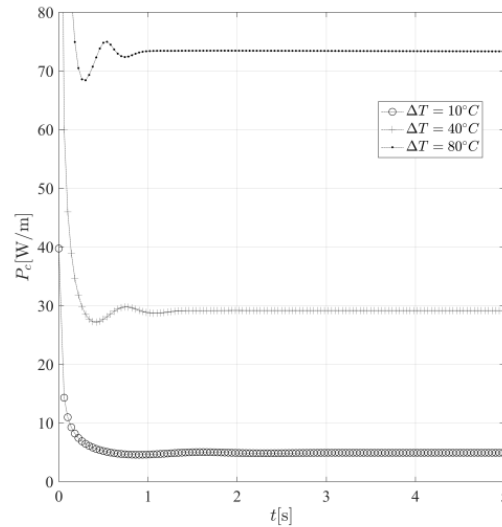
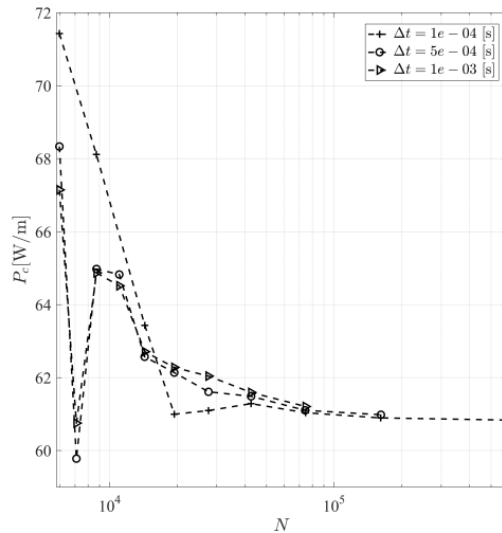




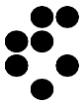
Simulation of natural convection from Al490Fe65 conductor



Steady state temperature profile of air at different skin-ambient temperature differences.

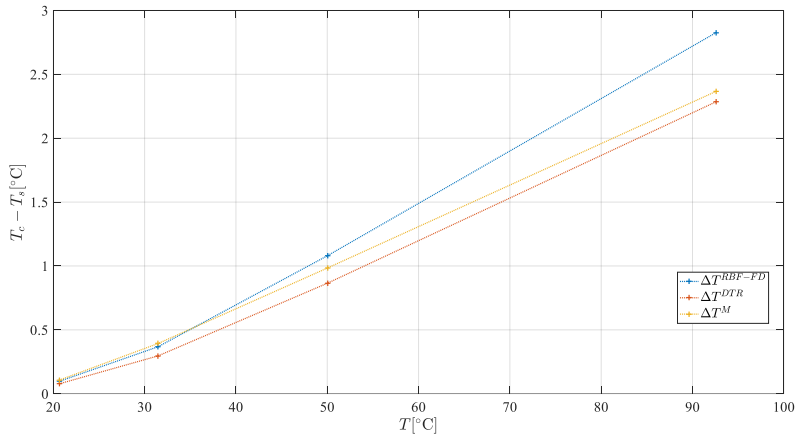
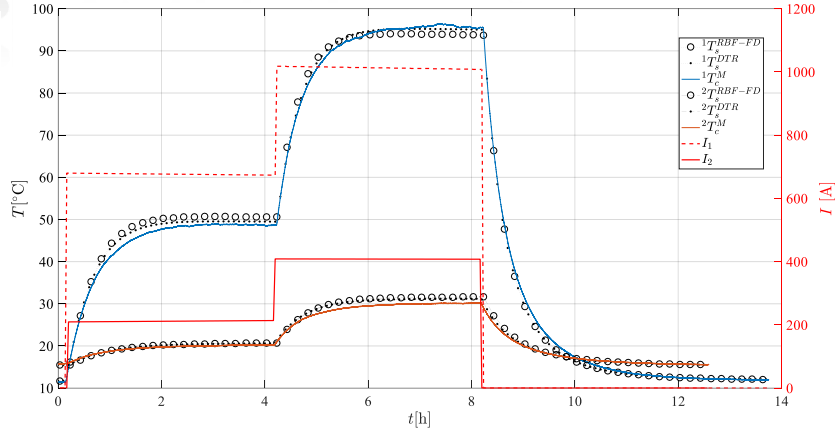


Convergence plot (left) and time development at different skin-ambient temperature differences

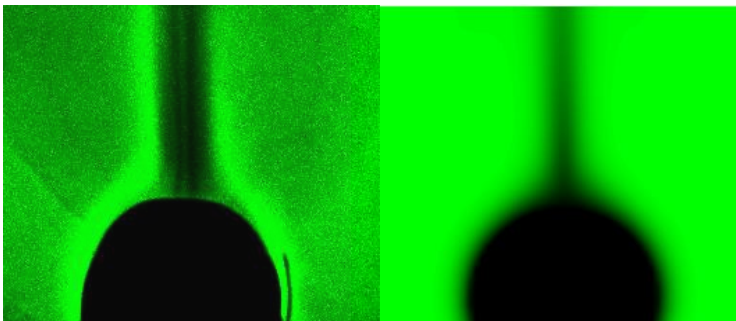


Validation of numerical simulation

RBF-FD – numerical simulation, M - measurement



Experimental setup for measurements of conductor temperature



Result of Schlieren photography Simulated temperature



Experimental setup for Schlieren photography.



Conclusions

Improving DTR algorithms

We prepared a numerical simulation of heat transport within the overhead line and thermo-fluid transport in surrounding air with the ultimate goal to further improve treatment of the most important cooling mechanism of overhead power line, i.e. convection.

The physical model is solved by an in-house implementation of RBF-FD method within the **Medusa** open source meshless project.

Model is validated by comparing simulation results, experimental data and IEEE and CIGRE standards.

Future work

Implement simulation of convective cooling in forced convection regime.

Prepare simulated relations for Nusselt number with respect to the wind velocity and geometry of the power line.

Thank you for your attention